Uncovering gene regulatory relationships from time-series expression data using networkBMA

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This document illustrates the use of the networkBMA R package (Fraley et al. 2012) to uncover regulatory relationships in yeast (Saccharomyces cerevisiae) from microarray data measuring time-dependent gene-expression levels in 95 genotyped yeast segregants subjected to a drug (rapamycin) perturbation.

1 Data

The expression data for this vignette is provided in the networkBMA package in the vignette database, which consists of three R objects:

timeSeries: A 582 by 102 data frame in which the first two columns are factors identifying the replicate and time (in minutes) after drug perturbation, and the remaining 100 columns are the expression measurements for a subset of 100 genes from the yeast-rapamycin experiment described in Yeung et al. (2011). There are 582/6 = 97 replicates (the 95 segregants plus two parental strains of the segregants), each with measurements at 6 time points. The complete time series data is available from Array Express (Parkinson et al. 2007) with accession number E-MTAB-412 (http://www.ebi.ac.uk/arrayexpress/experiments/E-MTAB-412).

reg.known: A 18 by 3 data frame giving known regulatory relationships among this subset of 100 genes. The first two columns give the regulator and target gene, respectively, while the third encodes the source of the regulatory information ('YPD' for Yeast Proteome Database (Hodges et al. 1999) and 'SCPD' for The Promoter Database of Saccharomyces cerevisiae (Zhu and Zhang 1999). In this example, we constrained reg.known to high-confidence experimental results obtained from biochemical (non-high-throughput) experiments.

reg.prob: A 100 by 100 matrix, giving probability estimates for regulatory relationships in which the (i, j) entry gives the estimated probability that gene i regulates gene j. These were computed using the supervised framework integrating multiple data sources of Lo et al. (2012).

referencePairs: A 2-column data frame giving 287 regulator-gene pairs among the selected set of 100 genes reported from the literature. In this yeast example, the reference network was extracted from the documented evidence from the YEASTRACT database (Teixeira et al. 2006), which includes curated regulatory relationships from the literature inferred from high-throughput experiments.

brem.data: An 85 by 111 subset of the data used for network inference in yeast (Brem et al. 2002, Brem and Kruglyak 2005). The rows correspond to genes and the columns to experiments. Provided courtesy of Rachel Brem.

```
> library(networkBMA)
```

- > data(vignette)
- > dim(timeSeries)
- [1] 582 102
- > dim(reg.prob)
- [1] 100 100
- > dim(brem.data)
- [1] 85 111
- > reg.known

	Regulator	TargetGene	source
1	YDR216W	YKR009C	YPD
2	YERO40W	YPL111W	YPD
3	YERO40W	YKL015W	YPD
4	YERO40W	YOR348C	YPD
5	YJR094C	YDR523C	YPD
6	YKL062W	YMR169C	YPD
7	YKL062W	YPL061W	YPD
8	YKL062W	YAL062W	YPD
9	YKL062W	YIL155C	YPD
10	YKL062W	YFL014W	YPD
11	YKL062W	YCR021C	YPD
12	YKL062W	YDR258C	YPD
13	YKL062W	YJR094C	YPD
14	YKL062W	YER150W	YPD
15	YKL062W	YNL194C	YPD
16	YBL103C	YNL037C	YPD
17	YKL112W	YCL064C	SCPD
18	YKL112W	YHRO51W	SCPD

2 Network Modeling

Given the yeast expression data from the Rapamycin experiments, the networkBMA function can be invoked to estimate the probabilities of regulatory relationships using either ScanBMA or iterative Bayesian Model Averaging (Yeung et al. 2005, 2011). The ScanBMA algorithm, as shown in Algorithm 1, is preferred when available. The parameter "prior.prob" indicates

the prior probabilities of regulatory relationships. If the parameter "prior.prob" is set to a single positive fraction, it represents the probability of a regulator-gene pair in the network (i.e. the expected network density as defined in (Lo et al. 2012)). The parameter "prior.prob" can also be set to a matrix in which the (i,j) entry is the estimated prior probability that gene i regulates gene j. The default value of "prior.prob" is NULL, which implies that no prior information will be used in modeling the network.

```
> edges.ScanBMA <- networkBMA(data = timeSeries[,-(1:2)],
                       nTimePoints = length(unique(timeSeries$time)),
+
                       prior.prob = reg.prob,
                       nvar = 50,
                       ordering = "bic1+prior", diff100 = TRUE, diff0 = TRUE)
> edges.ScanBMA[1:9,]
    Regulator TargetGene PostProb
1
      YJL217W
                 YJL217W
2
      YIL037C
                 YIL037C
                                  1
3
      YGL009C
                 YGL009C
                                  1
101
      YHR216W
                 YHR216W
                                  1
102
      YOLO14W
                 YOL014W
                                  1
                                  1
201
      YAL062W
                 YAL062W
202
      YHR136C
                 YHR136C
                                  1
                                  1
203
      YJR094C
                 YJR094C
301
      YORO32C
                 YORO32C
                                  1
```

For each gene g, the observed gene expression of genes at time t-1 serve as linear predictors for modeling the observed expression of gene g at time t. BMA modeling results in a weighted average of models consisting of relatively small numbers of predictors. The probability of gene h being a linear predictor in the model for gene g is taken as the probability that gene h regulates gene g in the network.

There are options for ordering the variables (parameter "ordering") and specifying the number of ordered variables (parameter "nvar") to be included in the modeling. In both algorithms ScanBMA and iBMA, all the candidate variables (genes) are initially ranked using the method specified in "ordering", and the top "nvar" such variables will be used as input in the BMA regression step. Note that if ScanBMA is used, the parameter "ordering" will have no effect in the BMA regression step.

Differentiation can also be performed on edges returned with 0% or 100% posterior probability. To include known regulatory relationships, the iBMA algorithm must be used. This can be done as shown below, but the results shown subsequently will use the call with ScanBMA as the algorithm, as above.

```
diff0 = FALSE)
> edges.iBMA[1:9,]
   Regulator TargetGene PostProb
     YBL103C
                 YBL103C
                                  1
1
2
     YNR053C
                 YBL103C
                                  1
3
     YOR206W
                 YBL103C
                                  1
4
     YKL112W
                 YKL112W
5
     YMR229C
                 YKL112W
8
     YDR216W
                 YDR216W
                                  1
9
     YDL170W
                 YDR216W
                                  1
10
     YOR302W
                 YDR216W
                                  1
11
     YPL265W
                 YDR216W
                                  1
```

Algorithm 1: ScanBMA

```
Initialize \mathcal{M}_{keep}, \mathcal{M}_{next} = \{\}
Initialize \mathcal{M}_{active} = \{null\ model\}, bestScore = 0
while \mathcal{M}_{active} not empty do

| for model\ m_{new} in NeighborsOf(\mathcal{M}_{active}) do
| mScore = \text{EvaluateModelScore}(m_{new})
| if mScore in OccamsWindow(bestScore) then
| | add m_{new} to \mathcal{M}_{next}
| bestScore = \text{BestModelScore}(bestScore, mScore)
| end
| end
| Trim models from \mathcal{M}_{keep} according to bestScore
| Add good models from \mathcal{M}_{active} to \mathcal{M}_{keep}
| \mathcal{M}_{active} = \text{good models from } \mathcal{M}_{next}
| end
| return \mathcal{M}_{keep}
```

3 Assessment of Network Models

Although, except for synthetic data, the true underlying network is unknown, the results can be assessed using a set of regulator-target gene network edges reported in the literature. The comparison is done as follows:

- Let E be the set of regulator-target gene edges resulting from networkBMA, possibly reduced using a probability threshold. In the context of the example in Section 2, E corresponds to the set of edges represented in the object edges.ScanBMA.
- Let K be the set of known regulator-target gene edges hardcoded in the modeling. In the example in Section 2, K corresponds to reg.known.

- Let L be the set regulator-target gene edges reported in the literature. In the example in Section 2, L corresponds to referencePairs.
- Let $E \setminus K$ and $L \setminus K$ be the set of pairs in E and L, respectively, with any hardcoded edges removed. In the example of Section 2, E represented by edges. ScanBMA contains 483 pairs, and L represented by referencePairs contains 287 pairs. Both E and L include all 18 of the known hardcoded edges K represented by reg.known. Hence $E \setminus K$ contains 465 pairs, and $L \setminus K$ contains 269 pairs.
- Let U be the set of all directed pairs r-g such that r is a regulator in $L \setminus K$ and g is a target gene in $L \setminus K$. For the example of Section 2, $L \setminus K$ has 11 unique regulator genes and 99 unique target genes. So there are 11×99 or 1089 pairs in U. Assume further that the linked pairs in U are precisely those pairs in $L \setminus K$, and that all other pairs are unlinked.
- Let $U \setminus K$ be the set of pairs in U with any hardcoded eggs removed (hardcoded edges may resurface in the unlinked pairs). For the example of Section 2, 17 of the 18 pairs in K occur in U, so there are 1089 17 = 1072 edges in $U \setminus K$.

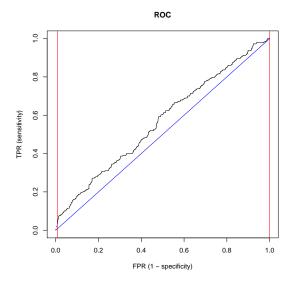
The assessment is done using the contingency table of $(E\backslash K)\cap (U\backslash K)$ relative to $U\backslash K$. For the example of Section 2, the assessment would be done with the 57 of the 465 pairs in $E\backslash K$ that also belong to $U\backslash K$.

A function called contabs.netBMA is provided to produce contingency tables from a reference network according the procedure described above. Here we compare the edges produced in Section 2 by networkBMA modeling on the yeast data with the reference network referencePairs made up of results reported in the literature:

Another function called 'contabs' is provided for computing contingency tables when the true underlying network is known. The scores function can be used to obtain common assessment statistics from the contingency tables, including sensitivity, specificity, precision, recall, and false discovery rate among other measures.

```
> scores( ctables, what = c("FDR", "precision", "recall"))

FDR precision recall
0.5 0.5384615 0.4615385 0.0669145
0.75 0.4705882 0.5294118 0.0669145
0.9 0.4193548 0.5806452 0.0669145
```



> title("Precision-Recall")

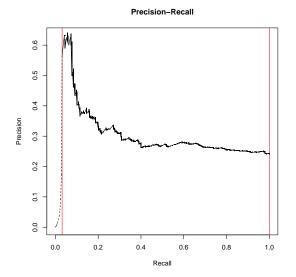


Figure 1: ROC and Precision-Recall curve sectors for a **networkBMA** model of the yeast-rapamycin test data. The black lines delineate the estimated curves. The vertical red lines delineate the range of horizontal values covered by the contingency tables. The dotted black lines are linear interpolants outside this range. The diagonal blue line on the ROC plot indicates the line between (0,0) and (1,1).

Areas under the ROC and Precision-Recall curves covered by contingency tables can also be estimated using functions roc and prc, with the option to plot the associated curves. The following gives the ROC and Precision-Recall curvers associated with the default contingency tables, in which the threshholds are all values for posterior probabilities that appear in edges.ScanBMA.

```
> roc( contabs.netwBMA( edges.ScanBMA, referencePairs), plotit = TRUE)
    area sector width
0.5649646 0.5637329 0.9911210
> title("ROC")
> prc( contabs.netwBMA( edges.ScanBMA, referencePairs), plotit = TRUE)
    area sector width
0.2925781 0.2910370 0.9686411
```

The resulting plots are shown in Figure 1. The output components are as follows:

- area: The estimated area under the curve for the horizontal sector ranging from 0 to 1. This should be used with caution when the sector in which the data falls is small.
- sector: The estimated area under the horizontal sector covered by the contingency tables.
- width: The width of the horizontal sector covered by the contingency tables.

4 Linear Modeling for Static Gene Expression Data

networkBMA relies on sparse linear modeling via iterative Bayesian model averaging (BMA). BMA addresses uncertainty in model selection, and builds a weighted—average model from plausible models. The resulting model has better overall predictive ability than constituent models, and tends to use few variables from among a larger set. BMA has been iteratively extended to data with more variables that observations (Yeung at al. 2005, 2009, 2011). The networkBMA package functions, ScanBMA and iterateBMAlm, for linear modeling via iterative BMA. We illustrate their use on a static gene expression dataset (without any time points), brem.data, to infer the regulators of a particular gene by regressing it on the expression levels of the other genes. Functions ScanBMA and iterateBMAlm can be applied to each gene so as to infer all edges in the network. For one gene, the procedure is as follows:

Function ScanBMacontrol facilitates input of BMA control parameters, including useg for indicating whether to use Zellner's g-prior or BIC for model likelihood approximation and OR for defining the width of 'Occam's window' for model exclusion. gCtrl allows specification of parameters related to the use of Zellner's g-prior, including whether to use a static g or optimize g using an EM algorithm. See the R help documentation for ScanBMacontrol and gControl for detailed description of these parameters, and Hoeting et al. (1999) for a tutorial on the underlying BMA paradigm. The estimated posterior probabilities (in percent) for genes that regulate YBL103C can be seen as follows:

> ScanBMAmodel.YNL037C\$probne0[ScanBMAmodel.YNL037C\$probne0 > 0]

YBL103C	YDL170W	YDR043C	YDR216W	YERO40W	YGL254W	YJR094C	YKL062W
15.81895	6.33311	17.25494	99.30193	5.31088	2.83664	1.58314	3.95383
YMR280C	YORO32C	YLR276C	YMR193W	YHRO51W	YPL111W	YGL009C	YPR002W
2.83050	5.24749	2.94435	1.39853	2.58522	2.79859	3.43629	100.00000
YML123C	YHR136C	YER158C	YJL217W	YKR075C	YLR258W	YDR171W	YIL136W
3.63262	1.38361	1.72177	1.60902	1.21411	100.00000	100.00000	99.72728
YKR056W	YAL062W	YCR021C	YDL110C	YGR043C	YGR142W	YHR018C	YJL088W
10.12298	100.00000	1.09232	1.36683	1.92756	1.74354	2.40810	1.29696
YJR148W	YLR009W	YLR130C	YLR267W	YLR327C	YNL036W	YNR053C	YOR302W
100.00000	3.22791	2.11767	1.29808	8.36596	1.45602	1.32398	1.24863
YPL012W	YIL037C	YKR009C	YFR022W	YPL265W	YOR100C	YOR348C	YHL028W
84.09918	1.23302	1.32936	100.00000	100.00000	99.41495	98.79002	1.40035
YGR067C	YLL011W	YPL036W	YAL054C	YLR438W	YIL155C	YBR054W	YCL064C
1.10718	1.88925	1.05122	5.08782	3.38030	1.36713	2.34692	100.00000
YDL160C	YDR384C	YERO67W	YER150W	YFL014W	YHR029C	YHR087W	YLR178C

1.26625	4.70142	2.49145	2.05581	5.76384	5.43642	1.91634	64.98200
YMR169C	YMR229C	YNRO64C	YOR206W	YOR388C	YDR380W	YPL061W	YJL172W
9.73588	100.00000	4.78895	2.77098	17.46033	1.91489	1.23917	1.45981
YNL194C	YDR361C	YHR216W	YNRO46W	YGR183C	YLL034C	YDR523C	YOLO14W
11.01615	4.27226	1.36634	1.15586	99.73287	36.44980	7.59316	3.15712
YLR174W	YJL153C	YGL229C	YJL063C				
1.52603	100.00000	100.00000	1.21337				

5 Acknowledgements

We would like to thank Dr. Roger Bumgarner for helpful discussion.

Funding: AER, KYY and WCY are supported by NIH grant 5R01GM084163. KYY is also supported by 3R01GM084163-05S1. AER is also supported by NIH grants R01 HD054511 and R01 HD070936, and by Science Foundation Ireland ETS Walton visitor award 11/W.1/I207.

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